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# Coherence of a field gradient driven singlet-triplet qubit coupled to multielectron spin states in $^{28}\text{Si}/\text{SiGe}$

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Younguk Song <sup>1,4</sup>, Jonginn Yun <sup>1,4</sup>, Jehyun Kim<sup>1</sup>, Wonjin Jang <sup>1</sup>, Hyeongyu Jang<sup>1</sup>, Jaemin Park<sup>1</sup>, Min-Kyun Cho <sup>1</sup>, Hanseo Sohn<sup>1</sup>, Noritaka Usami<sup>2</sup>, Satoru Miyamoto<sup>2</sup>, Kohei M. Itoh <sup>3</sup> & Dohun Kim <sup>1</sup> ✉

Engineered spin-electric coupling enables spin qubits in semiconductor nanostructures to be manipulated efficiently and addressed individually. While synthetic spin-orbit coupling using a micromagnet is widely investigated for driving and entangling qubits based on single spins in silicon, the baseband control of encoded spin qubits with a micromagnet in isotopically purified silicon has been less well investigated. Here, we demonstrate fast singlet-triplet qubit oscillation ( $\sim 100$  MHz) in a gate-defined double quantum dot in  $^{28}\text{Si}/\text{SiGe}$  with an on-chip micromagnet with which we show the oscillation quality factor of an encoded spin qubit exceeding 580. The coherence time  $T_2^*$  is analyzed as a function of potential detuning and an external magnetic field. In weak magnetic fields, the coherence is limited by frequency-independent noise whose time scale is faster than the typical data acquisition time of  $\sim 100$  ms, which limits the  $T_2^*$  below  $1 \mu\text{s}$  in the ergodic limit. We present evidence of sizable and coherent coupling of the qubit with the spin states of a nearby quantum dot, demonstrating that appropriate spin-electric coupling may enable a charge-based two-qubit gate in a (1,1) charge configuration.

Balancing the manipulation speed and coherence time, which often play opposing roles, has been a major goal of semiconductor quantum dot-based quantum information processing platforms<sup>1–3</sup> to maximize the qubit control fidelity. The electrical control of spin states is a representative example where, depending on the properties of the host material, either intrinsic<sup>4,5</sup> or extrinsic<sup>6,7</sup> spin-electric coupling methods have been explored. While strong spin-orbit coupling in compound semiconductors such as InAs and InSb enables fast Rabi oscillations<sup>4,5</sup>, the fluctuations of the nuclear bath or susceptibility to charge noise due to strong spin-orbit coupling limit the inhomogeneous coherence time  $T_2^*$  to the order of tens of nanoseconds. More recently, hole spins in group IV materials such as Ge (ref. 8) and Si (ref. 9) or electron spins in the Si-MOS structure<sup>10</sup> have been attracting much attention due to a more favorable ratio between the spin-orbit-based control speed and coherence time.

The electrons in silicon, in particular in the Si/SiGe heterostructure, have small intrinsic spin-orbit coupling<sup>11</sup>; therefore, an extrinsic method such as a micromagnet is necessary to rapidly manipulate its spin states. For single-spin qubits, the placement of an on-chip micromagnet has proven

effective for both natural<sup>7,12</sup> and isotopically enriched silicon<sup>13</sup> in Si/SiGe and Si-MOS structures, where the field gradient provides fast control while not severely compromising the spin coherence. In the case of the silicon-based two-electron singlet-triplet qubit, however, the efficiency of the technique involving a micromagnet has not been fully examined. Previous studies of singlet-triplet qubit operation either used a small field gradient<sup>14</sup> or relied on the modulation of the exchange energy<sup>15</sup> in natural silicon. Exploration of the micromagnet technique with a field gradient in the intermediate range in isotopically purified silicon would thus be important for optimizing spin-electric coupling. In addition, this approach would enable this route to be compared with other methods such as the recently demonstrated spin-valley-driven coherent singlet-triplet oscillation in silicon<sup>16,17</sup>.

Here, we demonstrate singlet-triplet qubit oscillation in a gate-defined double quantum dot in  $^{28}\text{Si}/\text{SiGe}$ . An on-chip micromagnet is used to generate a magnetic field gradient that is sufficient to allow fast manipulation (oscillation frequency  $f_Q \sim 100$  MHz), while benefiting from high spin coherence by isotopic enrichment. We measure the variation in the spin-electric coupling strength in the large valley-splitting regime ( $>175 \mu\text{eV}$ ) in

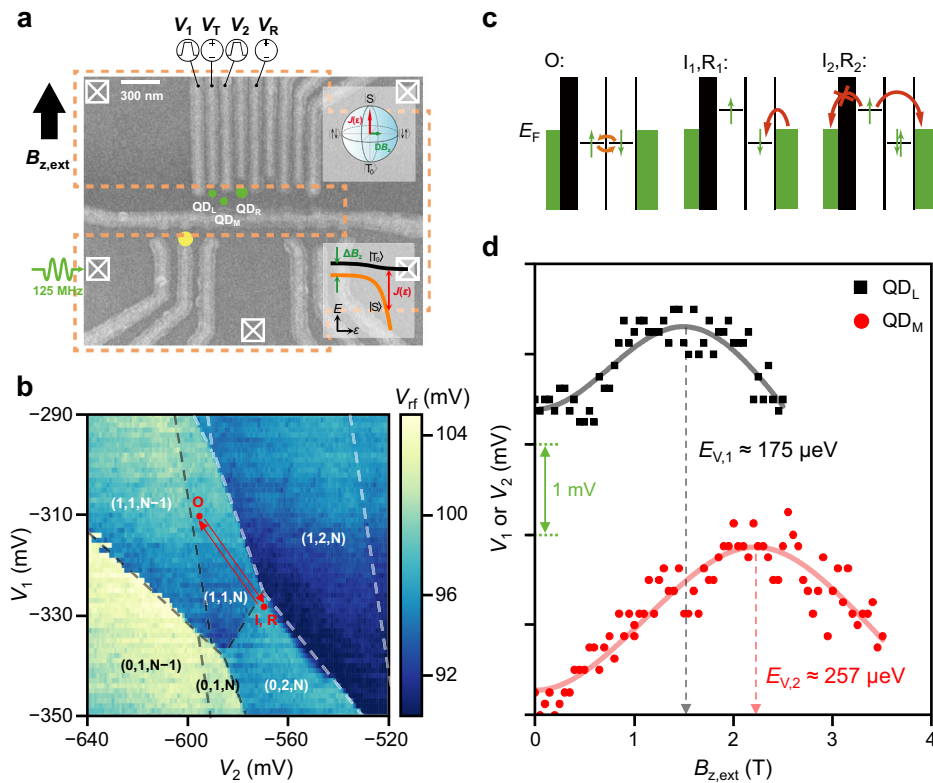
<sup>1</sup>Department of Physics and Astronomy, and Institute of Applied Physics, Seoul National University, Seoul, Korea. <sup>2</sup>Graduate School of Engineering, Nagoya University, Nagoya, Japan. <sup>3</sup>Department of Applied Physics and Physico-Informatics, Keio University, Yokohama, Japan. <sup>4</sup>These authors contributed equally: Younguk Song, Jonginn Yun. ✉e-mail: [dohunkim@snu.ac.kr](mailto:dohunkim@snu.ac.kr)

which an appropriate field gradient enables an encoded spin qubit to attain an oscillation quality factor over 580. We also present the analysis of the variation in  $T_2^*$  as a function of experimental parameters such as detuning  $\epsilon$ , magnetic field  $B_{z,\text{ext}}$ , and gate tuning conditions, exploring the origin of the dominant noise source in the system. Moreover, we present evidence that the qubit engages in sizable and coherent coupling with the spin states of a nearby quantum dot, thereby demonstrating that the appropriate amount of spin-electric coupling may enable a different type of two-qubit gates of encoded spin qubits.

## Results

### The triple quantum dot system

Figure 1a shows a multiple quantum dot device fabricated on top of a  $^{28}\text{Si}/\text{SiGe}$  heterostructure (see Methods for details of the material structure and device fabrication). We focus on a two-electron singlet-triplet ( $\text{ST}_0$ ) qubit formed by the gate electrodes near the left Ohmic contact and a global top gate (not shown) while the regions beneath the other electrodes are fully accumulated. The general Hamiltonian  $H$  of the  $\text{ST}_0$  qubit can be expressed as  $H = J(\epsilon)\sigma_z + \Delta B_z\sigma_x$ , where  $J(\epsilon)$  is an  $\epsilon$ -dependent exchange interaction with the Pauli matrix  $\sigma_{i=x,y,z}$ .  $\Delta B_z$  is the magnetic field difference between the quantum dots constituting the qubit and is denoted in the frequency unit Hz using  $Tg\mu_B/h$ , where  $g$ ,  $\mu_B$ , and  $h$  are the Lande  $g$ -factor of the electrons in silicon, the Bohr magneton, and Planck's constant, respectively.

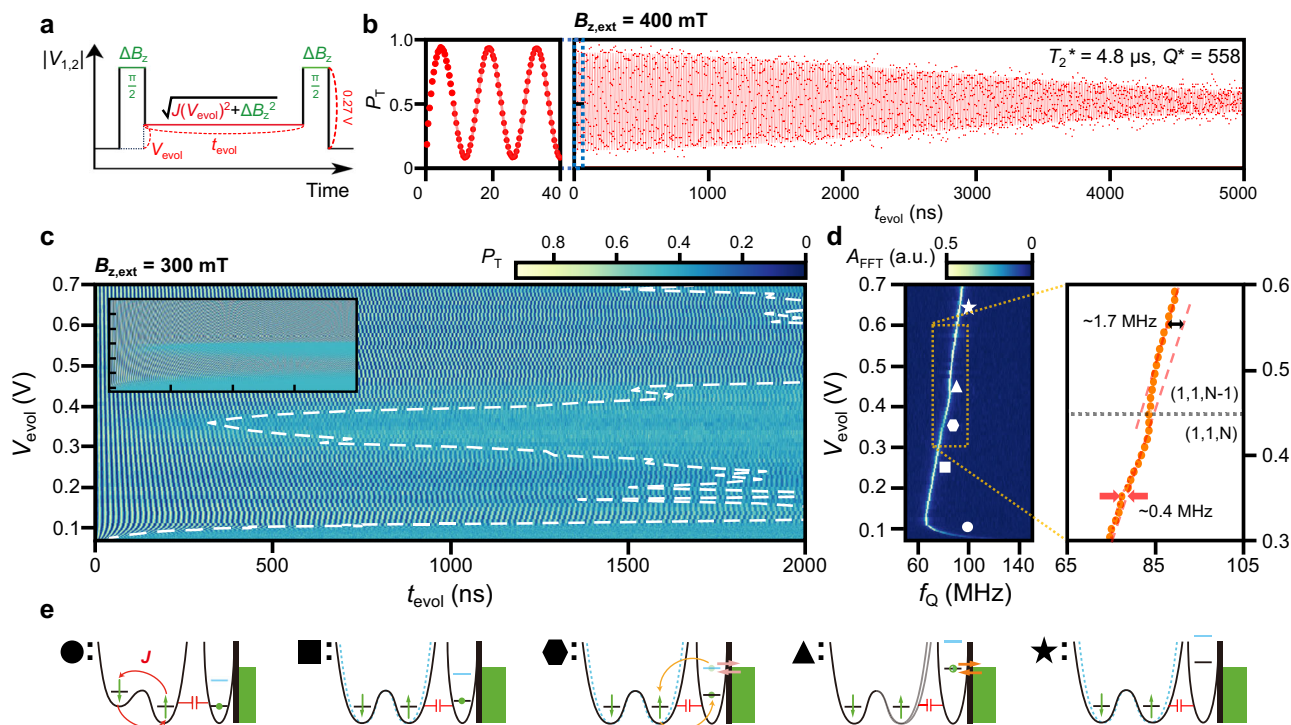


**Fig. 1 | The quantum dot device and triple quantum dot system.** **a** Scanning electron microscopy image of the device with the accumulation gates and Co micromagnet omitted. The black arrow indicates the direction of the external magnetic field  $B_{z,\text{ext}}$ . We focused on three quantum dots, indicated by the green dots labeled  $\text{QD}_L$ ,  $\text{QD}_M$ , and  $\text{QD}_R$ . We used  $\text{QD}_L$  and  $\text{QD}_M$  as the  $\text{ST}_0$  qubit and the many-electron dot  $\text{QD}_R$  to explore the coherent interactions with the  $\text{ST}_0$  qubit. High-frequency and synchronous voltage pulses combined with DC voltage were input to gates  $V_1$ ,  $V_2$ ,  $V_T$ , and  $V_R$  to tune and manipulate the quantum systems. The yellow dot indicates the sensor dot based on an RF single-electron transistor, with a transpassing RF signal of  $\sim 125$  MHz through RF Ohmic contact (indicated by the crossed squares). The orange dashed line indicates the micromagnet employed to apply a magnetic field difference  $\Delta B_z$  between  $\text{QD}_L$  and  $\text{QD}_M$ . The inset in the lower right corner illustrates the general energy level of the

Additionally, we formed a third, many-electron quantum dot next to the  $\text{ST}_0$  qubit to study the capacitive interaction between them. The design of the micromagnet on top of the device is similar to the ones used previously<sup>18</sup>. High frequency and synchronous voltage pulses, combined with the DC voltage through bias tees, were input to gates  $V_1$ ,  $V_2$ , and  $V_T$ . Fast RF reflectometry<sup>19,20</sup> was performed by injecting a carrier signal with a frequency of approximately 125 MHz and power of  $-100$  dBm at the Ohmic contact of the RF single-electron transistors on the left (see Fig. 1a). The reflected power was monitored through a chain of cryogenic and room temperature amplification and subsequent homodyne detection. The device was operated in a dilution refrigerator with a base temperature of approximately  $\approx 7$  mK, with  $B_{z,\text{ext}}$  ranging from  $-400$  mT to  $400$  mT applied in the direction shown in Fig. 1a.

Figure 1b shows the charge stability diagram of the  $\text{ST}_0$  qubit coupled with a many-electron quantum dot. The full specification of the number of electrons in the left, middle, and right quantum dots ( $\text{QD}_L$ ,  $\text{QD}_M$ ,  $\text{QD}_R$ , see green circles in Fig. 1a. For the position estimation sequence, see Supplementary Note 1) are denoted as  $(n,m,l)$ , whereas the  $(n,m)$  notation is used whenever we focus on the  $\text{ST}_0$  qubit only. A voltage pulse with a width of approximately 10 ns and rise time of 0.5 ns is input to  $V_1$  and  $V_2$  in the directions indicated by the red arrows in Fig. 1b. Near the charge transition from  $(0,2,N)$  to  $(1,1,N)$ , the pulse abruptly changes the Hamiltonian to the form  $H = \Delta B_z\sigma_x$ , where the spin state initialized to the

singlet and triplet states in a two-electron  $\text{ST}_0$  qubit, with  $\Delta B_z$  and detuning the  $\epsilon$ -dependent exchange interaction  $J(\epsilon)$ . The inset in the upper right corner depicts Bloch sphere representations of the contributions of  $J(\epsilon)$  and  $\Delta B_z$ , concerning the qubit rotation axis, with the two-electron states of the  $\text{ST}_0$  qubit. **b** Charge stability diagram of the primary operational region for  $\text{QD}_L$ ,  $\text{QD}_M$ , and  $\text{QD}_R$ . The number in parentheses represents the number of electrons in each of the three green dots. The inset shows  $V_{\text{CDS}}$ , the correlated double sampling signal of reflected RF signal  $V_{\text{rf}}$ . We drove the  $\text{ST}_0$  qubit to reach I-O-R sequentially by applying appropriate pulse sequences with  $V_1$  and  $V_2$ , while additional stopover points can be added to obtain the desired final qubit state. **c** Schematic of free evolution of the  $\text{ST}_0$  qubit in O and the initialize/readout sequence in the I/R points in (b), respectively. **d** Measurement of the valley splitting of  $\text{QD}_L$  and  $\text{QD}_M$  via magnetospectroscopy.



**Fig. 2 | The qubit dynamics revealed by Ramsey interferometry.** **a** Diagram of the pulse sequence used for Ramsey oscillation, the z-axis manipulation on the Bloch sphere with the free evolution time  $t_{\text{evol}}$ , and the pulse amplitude  $V_{\text{evol}}$ , with simultaneous control of  $|V_1|$  and  $|V_2|$ . A  $\pi/2$  pulse was applied with appropriately calibrated pulse duration time and  $V_{\text{evol}} = 0.27$  V, where the  $\Delta B_z$  contributes dominantly to the qubit rotation. **b** Representative Ramsey oscillation with the probability of the triplet state  $P_T$  at  $B_{z,\text{ext}} = 400$  mT and  $V_{\text{evol}} = 770$  mV, with high coherence time  $T_2^*$  and quality factor  $Q^*$  values. The results on the left and right were averaged 10,000 and 100 times, respectively. **c** Ramsey oscillations as a function of  $t_{\text{evol}}$  and  $V_{\text{evol}}$ . The white dashed line indicates the contour line of  $T_2^*$  extracted from each Ramsey oscillation line of  $V_{\text{evol}}$ . The inset shows the numerically

simulated Ramsey oscillation results. **d** Line-to-line fast Fourier transform (FFT) result of (c). The expected transition line of the dot on the right is indicated as a horizontal dotted line in the figure on the right. The two dashed orange lines show the linearly fitted  $f_Q$  with  $V_{\text{evol}}$  before and after the frequency shift of  $\Delta f_Q \sim 1.7$  MHz during the charge transition of  $\text{QD}_R$ . A small bump with maximum  $\Delta f_Q \sim 0.4$  MHz, indicated by the red arrows, is the footprint of the enhanced spin-dependent charge number fluctuation led by fast tunneling between  $\text{QD}_R$  and the electron reservoir on the right side of  $\text{QD}_R$ . **e** Schematic depicting the energy levels of each marker in (d), capacitive coupling between the  $\text{ST}_0$  qubit and  $\text{QD}_R$ , and the tunneling between  $\text{QD}_R$  and the electron reservoir.

singlet rotates around the  $x$ -axis on the Bloch sphere (Larmor oscillations<sup>11</sup>), thereby resulting in a non-zero triplet state probability  $P_T$ . The discrimination of the resultant excited state population is conventionally performed by Pauli spin-blockade (PSB)-based spin-to-charge conversion<sup>2,11,21</sup> where the singlet and triplet spin states are mapped to the (0,2) and (1,1) charge configurations, respectively. However,  $\Delta B_z$  produced by the micromagnet facilitates relaxation of the transient triplet (1,1) to the singlet (0,2) by mixing with the singlet (1,1) state, which makes a high-fidelity single-shot readout problematic<sup>22</sup>.

To circumvent the problem, we adopted one of the latched-PSB techniques that maps the triplet state to a long-lived metastable charge configuration<sup>23–25</sup>. Pioneered in a similar experiment performed in a GaAs triplet quantum dot system<sup>24</sup>, the version we used converts the triplet state (1,1) to the (1,2) state by rapidly loading an electron from the reservoir, which is expected to be located between  $\text{QD}_M$ ,  $\text{QD}_R$  and the gate displayed as the horizontal gray line in Fig. 1a, at a tunneling rate greater than the sensor bandwidth of 10 MHz (Fig. 1c, middle panel). On the other hand, tunneling to the reservoir on the left is tuned to be of the order of 10 Hz. At this rate, the metastable (1,2) state can relax to a singlet (0,2) state only by indirect and slow tunneling of an electron from  $\text{QD}_L$  to the reservoir on the right (Fig. 1c, rightmost panel). Along with the higher signal contrast of a charge of one electron compared with conventional PSB, the prolonged relaxation time of the triplet states enables fast and high-fidelity single-shot measurement. The fast measurement capability is also important to examine the extent to which the variation in the qubit coherence time depends on the total data acquisition time to determine the effect of slow charge noise<sup>26–28</sup>, as discussed in detail below.

Figure 1d shows the magnetospectroscopy measurements of the valley splitting<sup>29</sup> for  $\text{QD}_L$  and  $\text{QD}_M$ . By observing the crossover of the ground state from the singlet to the triplet by measuring the dependence of the energy required to add the second electron to each dot on  $B_{z,\text{ext}}$ , we obtain the valley splitting  $\sim 175$   $\mu\text{eV}$  (257  $\mu\text{eV}$ ) in  $\text{QD}_L$  ( $\text{QD}_M$ ). The result confirms that the valley splitting in our device is at the largest energy scale of at least twice that of the Zeeman splitting at the maximum  $B_{z,\text{ext}}$  applied in this study. Thus, we ignore the valley degree of freedom in this work and focus only on the  $\Delta B_z$ -driven  $\text{ST}_0$  qubit dynamics.

### Qubit dynamics driven by the field gradient

With the calibrated  $\pi/2$  pulse obtained from the Larmor oscillation measurement at the pulse amplitude  $|\Delta V_1| = |\Delta V_2| = 270$  mV, we construct a three-step pulse sequence for Ramsey interferometry (Fig. 2a). During the second step, at the pulse amplitude of free evolution  $V_{\text{evol}} = |\Delta V_1| = |\Delta V_2|$ , the qubit evolves around the axis of the Bloch sphere determined by the ratio of  $J(V_{\text{evol}})$  and  $\Delta B_z$ . Figure 2b shows a representative quantum oscillation at  $V_{\text{evol}} = 770$  mV under the representative tuning conditions. This demonstrates a record-high<sup>11,14,15</sup> oscillation quality factor  $Q^* = f_Q \times T_2^* = 116.25$  MHz  $\times$  4.8  $\mu\text{s} = 558$  of a  $\Delta B_z$ -driven  $\text{ST}_0$  qubit rotation in the deep (1,1) charge configuration. Although the  $Q^*$  tends to decrease as  $J(V_{\text{evol}})$  increases, the  $Q^*$  remains above 100 for  $J(V_{\text{evol}}) < 20$  MHz, the regime where we expect that the high-fidelity two-axis control of  $\text{ST}_0$  qubit can be implemented using AC driving<sup>15</sup>. In addition, high-resolution measurement (10,000 shots per data point with a single-shot readout time of 20  $\mu\text{s}$ ) of the first few

oscillations (Fig. 2b, left panel) shows a readout visibility of ~85% (see Supplementary Note 2 for details on the signal-to-noise ratio).

To more fully understand spin-electric coupling and its effect on the coherence time, we mapped the dependence on the free evolution time  $t_{\text{evol}}$  and  $V_{\text{evol}}$  of the Ramsey interference at  $B_{z,\text{ext}} = 300$  mT, as shown in Fig. 2c. The oscillation observed for  $V_{\text{evol}} < 0.1$  V shows the fast but short-lived oscillation driven by  $J$  (marked as ● in Fig. 2d and the corresponding schematic diagram in Fig. 2e), whereas the oscillations driven by  $\Delta B_z$  exhibit prolonged  $T_2^*$  (white dashed contour in Fig. 2c) for  $V_{\text{evol}} > 0.1$  V due to the lower charge noise susceptibility  $df_Q/dV_{\text{evol}}$ . In this regime, the data in the time and frequency domains exhibit the following main features. First,  $f_Q$  is generally linearly dependent on  $V_{\text{evol}}$ , which arises from the presence of the micromagnet (see ■ and ★ in Fig. 2d), and this is consistent with the previously observed linear shift of the single-spin resonance frequency in silicon in the presence of the synthetic field gradient<sup>13</sup>. Second,  $T_2^*$  depends non-monotonically on  $V_{\text{evol}}$ . In particular, a significant decrease in  $T_2^*$  is observed in the vicinity of  $V_{\text{evol}} = 0.35$  V (near ● in Fig. 2d). Third,  $f_Q$  undergoes an abrupt frequency shift of about  $\Delta f_Q \sim 1.7$  MHz at approximately  $V_{\text{evol}} = 0.45$  V (▲ in Fig. 2d). Estimated from the calibrated lever arm of 0.023, the cross-talk effect of  $V_{\text{evol}} = 0.45$  V on  $\text{QD}_R$  shifts the chemical potential of  $\text{QD}_R$  to the Fermi-level of the right contact  $E_F$  where the ground state charge transition occurs. Therefore, the observed  $\Delta f_Q \sim 1.7$  MHz per one electron change is the measurement of the capacitive coupling between the  $\text{ST}_0$  qubit and  $\text{QD}_R$ . We additionally verified this interpretation by adjusting the DC tuning of the plunger gate of  $\text{QD}_R$  and by observing the systematic shifts of the point ▲ (see Supplementary Note 3).

In general, the charge fluctuation in  $\text{QD}_R$  adversely affects the coherence of the capacitively coupled qubit. However, we note that  $V_{\text{evol}} = 0.35$  V (near ● in Fig. 2d) showing the lowest  $T_2^*$  occurs below  $V_{\text{evol}} = 0.45$  V (▲ in Fig. 2d) where  $\text{QD}_R$  experiences the maximum charge fluctuation. Assuming that non-negligible spin-dependent coupling occurs between the  $\text{ST}_0$  qubit and the Zeeman-split ground and excited spin states in  $\text{QD}_R$  occupied by  $N$  electrons ( $E_g$  and  $E_e$ , respectively), the qualitative interpretation of this phenomenon is as follows (See Supplementary Note 4 for data supporting spin-dependent coupling). For detuning near ■, the spin state in  $\text{QD}_R$  remains in the ground state with high fidelity as both  $E_g$  and  $E_e$  are well below  $E_F$ , and the spin-dependent charge fluctuation is low. From point ■ to ▲, as  $E_e$  approaches and passes  $E_F$ , fast tunneling between  $\text{QD}_R$  and the reservoir through  $E_e$  leads to enhanced spin-dependent charge number fluctuation. This fluctuation reduces  $T_2^*$  and produces a small frequency shift of  $\Delta f_Q \sim 0.4$  MHz (red arrows in Fig. 2d). In this regime, the spin state in  $\text{QD}_R$  is expected to be a mixed state because of the non-negligible average occupation in  $E_e$ . The maximum charge fluctuation, hence the minimum  $T_2^*$ , is expected to occur when  $E_e$  approximates  $E_F$ , which corresponds to the point ●. Finally, at point ▲,  $E_g$  aligns with  $E_F$ , resulting in the change in the full electron number in  $\text{QD}_R$  and the appearance of the kink in time-averaged  $f_Q$  measurement.

More quantitatively, we compared the experimental results with those of the numerical simulation<sup>30</sup> using the following phenomenological Hamiltonian and Lindblad operators, which were built based on the systematic analysis of Ramsey interferometry of the  $\text{ST}_0$  qubit discussed in the next section.

$$\begin{aligned} H &= J(V_{\text{evol}})\sigma_z \otimes \mathbf{1} + \Delta B_z(V_{\text{evol}})\sigma_x \otimes \mathbf{1} \\ &\quad + \beta(V_{\text{evol}})\mathbf{1} \otimes \sigma_z + \gamma(B_{z,\text{ext}})\mathbf{1} \otimes \sigma_x \\ &\quad + J_{\text{int}}(V_{\text{evol}})\frac{1}{e^{\eta(|V_{\text{evol}}| - \tau_1)} + 1}\sigma_x \otimes \sigma_z L_1 = \tau_1 \sqrt{J(V_{\text{evol}})}\sigma_z \otimes \mathbf{1}, L_2 \\ &= \tau_2 \sqrt{\beta(V_{\text{evol}})}\mathbf{1} \otimes \sigma_z \end{aligned} \quad (1)$$

Here, the Hamiltonian describes the two interacting qubits,  $\text{ST}_0$  qubit, and the two spin states of the nearby  $N$ -electron quantum dot,  $\text{QD}_R$ . More specifically, the Hamiltonian of the  $\text{ST}_0$  qubit is constructed as  $J(V_{\text{evol}})\sigma_z + \Delta B_z(V_{\text{evol}})\sigma_x$ , where the background  $\Delta B_z(V_{\text{evol}}) = 47.7 V_{\text{evol}} + 61.3$  ( $0.25 \text{ V} < V_{\text{evol}} < 0.7 \text{ V}$ ) is estimated from Fig. 2d. We assumed that the Hamiltonian of  $\text{QD}_R$  is analogous to that of the  $\text{ST}_0$  qubit, such that the

diagonal term  $\beta(V_{\text{evol}})$  is an exponential function of  $V_{\text{evol}}$ , and the off-diagonal term  $\gamma(B_{z,\text{ext}})$  is a linear function of  $B_{z,\text{ext}}$ . Furthermore, the coupling we consider is the spin-electric coupling induced from the spatial distribution of the orbital wavefunction of  $\text{QD}_R$  depending on its spin states. In view thereof, we chose the spin-electric coupled eigenstate of  $\text{QD}_R$  as the  $\sigma_z$  basis and introduced the interaction between the  $\text{ST}_0$  qubit and  $\text{QD}_R$ , which was assumed to be in the form of  $\sigma_x \otimes \sigma_z$ . This coupling term is multiplied by a phenomenological Fermi–Dirac distribution with proper constant  $c, \eta$  and coupling strength  $J_{\text{int}}(V_{\text{evol}})$  and to incorporate the change in the charge state of the nearby  $N$ -electron quantum dot (see Supplementary Note 5 for details of the simulation). Additionally, the phenomenological Lindblad operators for the  $\text{ST}_0$  qubit ( $L_1$ ) and two-level system in  $\text{QD}_R$  ( $L_2$ ) are introduced with the proportionality constant  $\tau_1$  ( $\tau_2$ ) to reflect the experimentally observed decoherence.

The inset in Fig. 2c shows the simulation result which consistently reproduces the sudden kink in the frequency near  $V_{\text{evol}} = 0.45$  V, the significant decrease in  $T_2^*$  near  $V_{\text{evol}} = 0.35$  V, and the subsequent recovery of  $T_2^*$  near the kink. Overall, by comparing the result of the simulation with that of the experiment, we concluded that the kink in the frequency and the drop in  $T_2^*$  indicate capacitive coupling between the  $\text{ST}_0$  qubit and  $\text{QD}_R$  during the charge transition of  $\text{QD}_R$ .

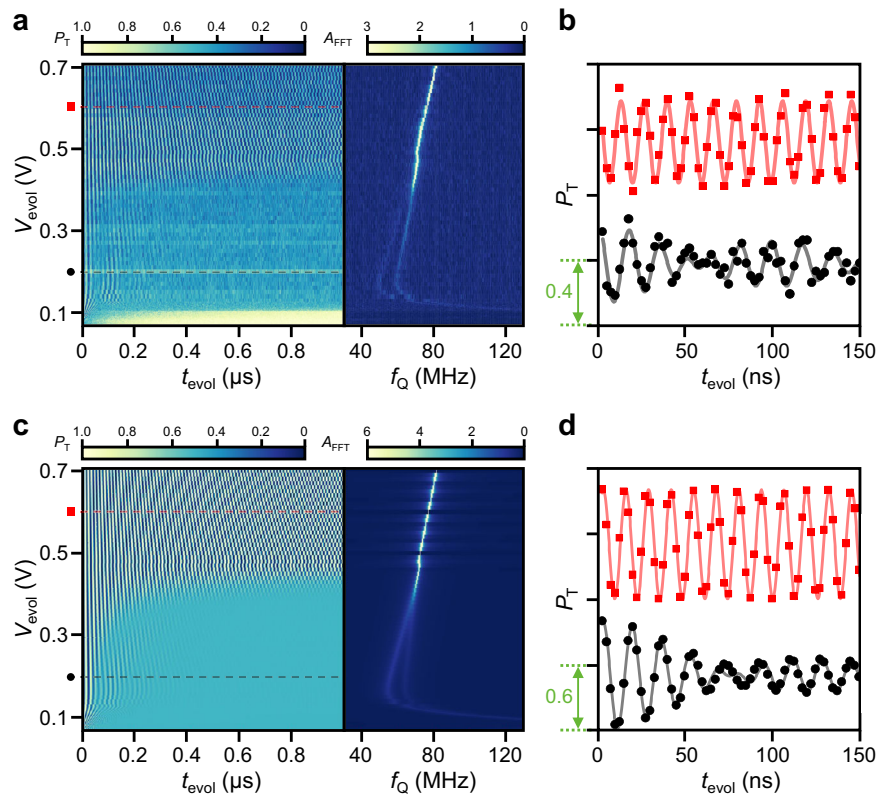
### Coherent coupling between $\text{ST}_0$ qubit and many-electron spin states

We further substantiated the validity of the above analysis by showing that the experimental and simulation results were consistently comparable under different quantum dot tuning conditions. Specifically, we fine-tuned the gate voltage levels to induce significant deviations in the overall coupling strength and the decoherence rates compared with the previous tuning condition. To establish the desired tuning condition, we primarily adjusted the gate  $V_R$  of Fig. 1a. In detail, while maintaining the optimal experimental parameters for qubit readout, we applied more negative voltage to the gate  $V_R$ , which is expected to increase  $J_{\text{int}}$  by decreasing the distance between  $\text{QD}_M$  and  $\text{QD}_R$ . In this new tuning, we observed the characteristic beating of the quantum oscillation below  $V_{\text{evol}} < 0.42$  V, as shown in Fig. 3a. Notably, the coherence of the oscillation markedly diminished when the coupling between the two qubits became appreciable. Figure 3b enables a more detailed examination of these results and provides the line cuts that offer a clearer comparison between the oscillation traces in the uncoupled ( $V_{\text{evol}} = 0.6$  V, top trace in Fig. 3b) and coupled ( $V_{\text{evol}} = 0.2$  V, bottom trace in Fig. 3b) regimes.

The Ramsey interferometry of the  $\text{ST}_0$  qubit reveals the structure of the multielectron state in  $\text{QD}_R$ . The observed beating oscillation of the  $\text{ST}_0$  qubit and the split of the corresponding FFT peak into two suggest that the multielectron state of  $\text{QD}_R$  is either a superposition or a mixed state of two different eigenstates. The interferometry of the  $\text{ST}_0$  qubit under different  $B_{z,\text{ext}}$  (see Supplementary Note 4 for the low  $B_{z,\text{ext}}$  result) shows that the degree of beating decreases and eventually disappears as  $B_{z,\text{ext}}$  decreases, revealing that the degree of mixing of the two  $\text{QD}_R$  states is inversely proportional to  $B_{z,\text{ext}}$ . Furthermore, the dependence of the beating of the oscillation on  $V_{\text{evol}}$  suggests that the degree of mixing of the eigenstates of  $\text{QD}_R$ , whose orbital wavefunction directly couples with  $f_Q$  through spin-electric coupling, is a function of  $V_{\text{evol}}$ . The significant drop in  $T_2^*$  in the regime of sizeable coupling is again likely a consequence of the interplay between the interqubit coupling and the dephasing effect discussed in the previous section. Nonetheless, the interqubit coupling rate is faster than the decoherence rate, suggesting the possibility of entangling an  $\text{ST}_0$  qubit with the multielectron level in  $\text{QD}_R$ . Additionally, the coupling strength with the maximum value of approximately 10 MHz also exhibits a dependence on  $V_{\text{evol}}$ , highlighting the electrical tunability of the interqubit coupling strength. The phenomenological Hamiltonian we introduced in the previous section summarizes these findings.

This experimental result was compared with the numerical simulation, which employed the identical Hamiltonian and Lindblad operators introduced in the previous section, whose parameters were appropriately

**Fig. 3 | Coherent coupling between the singlet-triplet qubit and many-electron spin states.** **a** Left: Ramsey oscillations as a function of  $t_{\text{evol}}$  and  $V_{\text{evol}}$  for different tuning levels. Significant dephasing appears below  $V_{\text{evol}} = 0.42$  V. Right: FFT result of the figure on the left. The FFT peak exhibits the characteristic kink near  $V_{\text{evol}} = 0.5$  V and linear dependence on  $V_{\text{evol}}$  in the  $\Delta B_z$ -dominating regime. Characteristic splitting of the FFT peak is also manifested below  $V_{\text{evol}} = 0.42$  V. **b** Ramsey oscillation trace at  $V_{\text{evol}} = 0.6$  V (top, red squares) and 0.2 V (bottom, black solid circles). The beating of the oscillation at  $V_{\text{evol}} = 0.2$  V is manifested. Each trace corresponds with the dashed line in the respective color in (a). The traces are offset by 1 for clarity. **c** Left: Numerical simulation of Ramsey oscillations as a function of  $t_{\text{evol}}$  and  $V_{\text{evol}}$ . The significant decoherence below  $V_{\text{evol}} = 0.42$  V was reproduced consistently. Right: FFT result of the figure on the left. The FFT peak shows the kink near  $V_{\text{evol}} = 0.5$  V, a  $V_{\text{evol}}$  dependence similar to the experimental results, and the characteristic splitting below  $V_{\text{evol}} = 0.42$  V. **d** Simulated Ramsey oscillation trace at  $V_{\text{evol}} = 0.6$  V (top, red squares) and 0.2 V (bottom, black solid circles). The simulated oscillation trace also reflects the beating of the oscillation at  $V_{\text{evol}} = 0.2$  V. Each trace corresponds with the dashed line in the respective color in (c). The traces are offset by 1.2 for clarity.

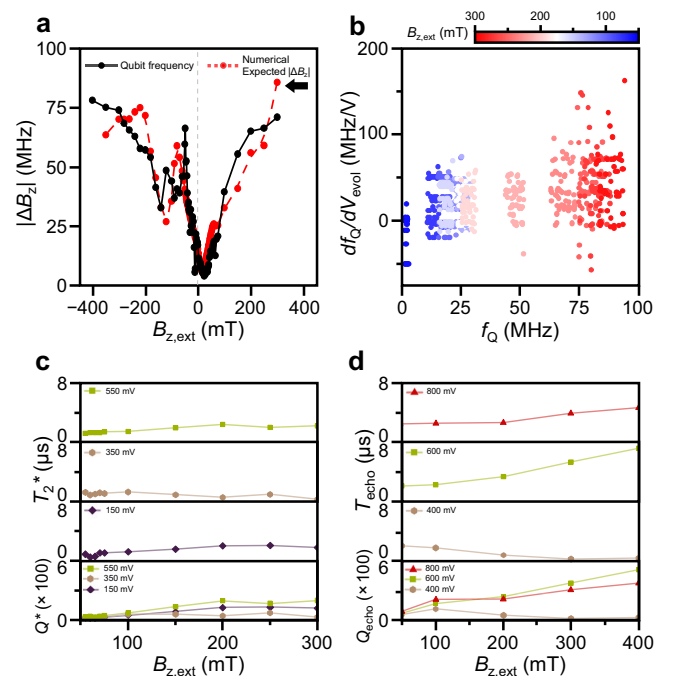


adjusted to reflect the different tuning conditions. One of the key adjustments involves the parameters of  $\beta(V_{\text{evol}})$ , which effectively transform the eigenstate of  $\text{QD}_R$  into the superposition of the  $\sigma_z$ -eigenstates for  $V_{\text{evol}} < 0.4$  V, which gives rise to the observed beating of the oscillation through the spin-electric coupling  $\sigma_x \otimes \sigma_z$  term. The numerical calculation consistently reproduces the experimental results, including the characteristic kink near  $V_{\text{evol}} = 0.48$  V, the emergence of the beating, and the significant reduction in  $T_2^*$  throughout the coupling regime. These observations can be attributed to the mixed eigenstate of  $\text{QD}_R$  and the Lindblad operators, which effectively mimic the aforementioned dephasing effect. Overall, our spin-electric coupling scenario convincingly reproduces the experimental results for various coupling parameters.

### External field dependence of $\text{ST}_0$ qubit coherence

We turn to discuss the dominant noise source limiting the coherence of  $\text{ST}_0$  qubit by investigating the variation in  $f_Q$  and  $df_Q/dV_{\text{evol}}$  as a function of  $B_{z,\text{ext}}$ . The magnitude of the field gradient  $|\Delta B_z|$  is determined by measuring  $f_Q$  of the  $\Delta B_z$ -dominated Ramsey oscillations at  $V_{\text{evol}} = 800$  mV for various values of  $B_{z,\text{ext}}$  from 400 mT to  $-400$  mT (Fig. 4a). Generally,  $|\Delta B_z|$  was positively correlated with  $B_{z,\text{ext}}$  which likely originated from the formation of multiple domains due to the demagnetization of the Co micromagnet at low  $B_{z,\text{ext}}$ . The calculated value expected for  $|\Delta B_z|$  by simulation of the magnetic field using the Object Oriented Micromagnetic Framework (OOMMF)<sup>31,32</sup> was in qualitative agreement with the experimental observation. (see Supplementary Note 6 for details of the micromagnetic simulation).

The controllability of  $|\Delta B_z|$  via  $B_{z,\text{ext}}$  paved the way to test whether a decrease in  $|\Delta B_z|$  could lead to a smaller  $df_Q/dV_{\text{evol}}$  and, consequently, an improved  $T_2^*$  at low  $B_{z,\text{ext}}$ . Figure 4b shows the dependence of  $df_Q/dV_{\text{evol}}$  on  $f_Q$ , extracted at various levels of  $B_{z,\text{ext}}$  and  $V_{\text{evol}}$ . Unexpectedly, a strong correlation did not exist between  $f_Q$  and  $df_Q/dV_{\text{evol}}$ . Depending on the experimental iteration,  $df_Q/dV_{\text{evol}}$  was widely dispersed even at similar  $f_Q$  controlled by  $V_{\text{evol}}$ . We again attribute this to the nanoscale formation of



**Fig. 4 | External magnetic field dependence of coherence time.** **a** Estimated  $|\Delta B_z|$  extracted from  $f_Q$  of the Ramsey oscillation performed for  $V_{\text{evol}} = 800$  mV in the  $\Delta B_z$ -dominating region (black), and expected  $|\Delta B_z|$  from the magnetic field simulation using OOMMF (red) (see Supplementary Note 6). The black arrow indicates the direction of the measurement. **b** Extracted  $f_Q$  and charge susceptibility  $df_Q/dV_{\text{evol}}$  of the qubit in  $B_{z,\text{ext}}$  of 300–40 mT and  $V_{\text{evol}}$  of 0.4–0.7 V.  $df_Q/dV_{\text{evol}}$  was derived with interpolated  $f_Q$ . **c** Measured  $T_2^*$ ,  $Q^*$  of the Ramsey oscillations as a function of  $B_{z,\text{ext}}$  at various  $V_{\text{evol}}$ . **d**  $T_{\text{echo}}$  and  $Q_{\text{echo}}$ , the results of the spin-echo experiment of  $T_2^*$  and  $Q^*$ , respectively, as a function of  $B_{z,\text{ext}}$  at various  $V_{\text{evol}}$ .

multiple domains in the micromagnet, which generates a locally inhomogeneous field distribution.

Figure 4c shows  $T_2^*$  and  $Q^*$  as functions of  $B_{z,ext}$  at several  $V_{evol}$ . Generally, the decreasing  $Q^*$  is predominantly the result of the rapid decrease in  $f_Q$  as the applied magnetic field  $B_{z,ext}$  weakens, whereas  $T_2^*$  varies at most by a factor of two as a function of  $B_{z,ext}$ . The latter finding is also consistent with the observation that  $f_Q$  and  $df_Q/dV_{evol}$  are not strongly correlated. Although  $T_2^*$  tends to increase in the presence of strong  $B_{z,ext}$ , we argue that this is because of the interplay between the experimental data acquisition time and dominant noise band, which shifts to the low frequency at stronger  $B_{z,ext}$ . We confirm that extending the total data acquisition time significantly affects  $T_2^*$  at  $B_{z,ext} = 400$  mT, indicating that slow charge noise compared to a given measurement time plays an important role (see Supplementary Note 7). Moreover, near  $V_{evol} = 350$  mV, where  $T_2^*$  is limited by strong coupling with the spin states in  $QD_R$  and fast charge noise is therefore presumed to dominate the noise spectrum,  $T_2^*$  is nearly constant as a function of  $B_{z,ext}$ . In this respect, we assume that  $T_2^*$  at low  $B_{z,ext}$ , which approximates  $1 \mu\text{s}$  regardless of the value of  $V_{evol}$ , is entirely dominated by the noise spectrum, which is faster than the measurement time. This indicates that the coherences of the  $ST_0$  qubit are closer to the ergodic limit.

The dominance of high-frequency noise in our system is also supported by measurement of the spin-echo time  $T_{echo}$  and echoed quality factor  $Q_{echo}$  at various  $B_{z,ext}$  and  $V_{evol}$  (Fig. 4d). Notably, the spin-echo enables only a minor improvement in the coherence time by a factor of at most two compared with  $T_2^*$  at low  $B_{z,ext}$  of  $\sim 100$  mT, thereby indicating that the major source of noise in this regime is in the high-frequency band. Similar ineffectiveness of the spin-echo was observed in a  $^{29}\text{Si}/\text{SiGe}$ -based singlet-triplet qubit for non-negligible  $J$  (ref. 33). Although a previous study<sup>34</sup> pointed out that the increased flip-flop motion of residual  $^{29}\text{Si}$  nuclear spins at low  $B_{z,ext}$  leads to the reduction of  $T_2^*$ , we rule out this possibility since we expect that the nuclear spin flip-flop rate is suppressed below 10 Hz by the presence of on-chip micromagnet<sup>35,36</sup>. Moreover, this type of noise is more likely to occur under RF excitations needed for single-spin qubit manipulation. The absence of such control in this experiment also indicates that the mechanism of the dominant noise source at low  $B_{z,ext}$  in our experiment differs from that in the previous study. The spin-echo more effectively enhances the coherence time at high  $B_{z,ext} > 300$  mT, which is consistent with our scenario that, in this regime, the dominant noise primarily stems from the low-frequency band. Similar to the behavior of  $T_2^*$ , the spin-echo is not effective when the  $ST_0$  qubit is strongly coupled with  $QD_R$  (see Fig. 4d, third panel).

We additionally compared the power spectral density (PSD) of noise for strong and weak magnetic fields,  $B_{z,ext}$  (400 and 50 mT, respectively) obtained by the single-shot measurement-based rapid Bayesian estimation method<sup>26,37,38</sup> (see also Supplementary Note 8) as shown in Fig. 5a. Although both of these spectra exhibit a larger white noise component compared to previous studies<sup>28,33</sup>, the PSD of the spectrum at  $B_{z,ext} = 50$  mT is about two orders of magnitude larger across the entire range of frequencies with

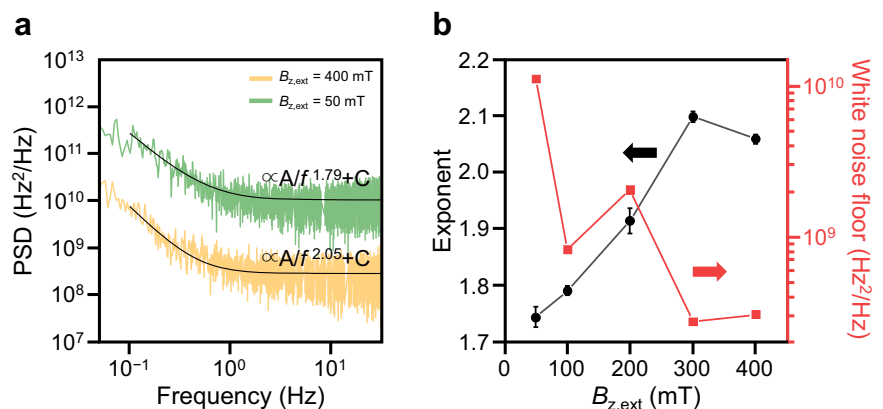
different exponent  $\alpha$  of the  $1/f^\alpha$ -like power spectrum compared to the PSD at  $B_{z,ext} = 400$  mT. Assuming that the frequency-independent noise extends to frequencies beyond the experimentally measured limit of  $\sim 40$  Hz, the result explains the overall ineffective noise refocusing via the spin-echo technique in our system, in particular at low  $B_{z,ext}$ . In addition, the tendency of the white noise floor to increase with decreasing  $B_{z,ext}$  along with the change in  $\alpha$  (Fig. 5b), which is generally indicative of a relative increase in the portion of fast charge noise, is consistent with the variation in  $T_2^*$  and  $T_{echo}$ , as presented in Fig. 4.

## Discussion

The origin of the rather high white noise floor in our system, which further increases at low  $B_{z,ext}$ , remains an open question. Although a more comprehensive understanding of the dominant noise source would require further experiments, the ineffective coherence recovery using the spin-echo technique due to relatively fast noise indicates that the noise does not predominantly originate from the increased flip-flop rate of the residual  $^{29}\text{Si}$  nuclear spins. Based on our investigation of the signature of the nanoscale multi-domain structure as the micromagnet demagnetizes at  $B_{z,ext} < 200$  mT, we speculate that the fast noise could have stemmed from the interplay between the field inhomogeneity induced by the magnetic domain structure and charge noise. This could be clarified by studying multiple devices containing micromagnets with various magnetic properties. A potential approach could involve the use of different techniques for micromagnet fabrication; for example, the deposition of magnetic material in the presence of an applied magnetic field, which is known to induce a preferential magnetization axis and hence a significantly modified hysteresis loop<sup>39</sup>. This technique may enable the magnetic structure to be more stably controlled in a weak magnetic field, which would allow an investigation of the transduced noise with varying magnetic properties. Moreover, the technique could also be useful for other applications such as semiconductor-superconductor hybrid circuits<sup>40,41</sup> for long-range coupling where operation in a weak magnetic field is beneficial.

Nevertheless, we successfully demonstrated coherent  $ST_0$  oscillations with outstanding  $Q^*$ . This was enabled by using an on-chip micromagnet technique in an isotopically purified  $^{28}\text{Si}/\text{SiGe}$  heterostructure where  $f_Q$  is tunable in the (1,1) charge configuration due to the dependence of the magnetization on  $B_{z,ext}$ . Our findings reveal that capacitive coupling can facilitate coherent interactions between two quantum systems: the two-electron  $ST_0$  qubit and the many-electron quantum dot. Moreover, by formulating Hamiltonians for these quantum systems and their interactions, we effectively reproduced the coherent  $ST_0$  qubit oscillation observed in our experiments through numerical simulation. Our work also suggests areas for improvement. Even though our device was designed to allow us to coarsely tune the chemical potential of  $QD_R$ , independent control of the quantum states of  $QD_R$  was challenging because of the limited number of control lines in the current single-gate layer structure. Enhanced control over individual quantum dots and precise coupling strength modulation

**Fig. 5 | Noise spectrum analysis.** **a** Noise spectrum acquired by applying two different  $B_{z,ext}$ . Power spectral densities (PSDs) were derived by analyzing single-shot data with the rapid Bayesian estimation method (see Supplementary Note 8). Each noise spectrum was calculated using 100,000 single shots. Offsets were excluded from this figure. **b** Power-law exponent and white noise floor level obtained from the noise spectrum at each  $B_{z,ext}$ .



could be attained by adopting an overlapped gate structure<sup>42</sup>, which may enable different two-qubit gate schemes for encoded spin qubits in silicon.

## Methods

### Material structure and device fabrication

The <sup>28</sup>Si/SiGe heterostructure wafer was grown by a molecular beam epitaxy growth method. An isotopically purified silicon source (with a residual <sup>29</sup>Si concentration of approximately 800 ppm) was used for the strained quantum well with a thickness of 12 nm. The design of the surface gate electrode resembles that of GaAs spin qubit devices where both quantum dot confinement and barrier gates reside in the same layer and a global accumulation gate is used for electrostatic doping. The dimensions of the accumulation gate were maintained below  $2 \times 2 \mu\text{m}^2$  to minimize the parasitic capacitance<sup>20</sup>, enabling proper impedance matching conditions for radio frequency (RF) reflectometry. A Co micromagnet was deposited above the accumulation gate using an e-beam evaporator, with a Au cap for the antioxidation layer.

### Measurement setup

The sample was cooled to the base temperature,  $\sim 7$  mK, with a cryogen-free dilution refrigerator (Oxford Instruments Triton-500). A sensing dot based on an RF single-electron transistor was used to detect the change in the charge state of QD<sub>L</sub>, QD<sub>M</sub>, and QD<sub>R</sub> in our system. An onboard inductor of 1500 nH and a parasitic capacitance on the order of 1 pF formed an LC-tank circuit with a resonance frequency at  $\sim 125$  MHz, which was used for RF reflectometry. Two arbitrary waveform generators (HDAWG and Operator-X+ by Zurich Instruments and Quantum Machines, respectively) were used to synchronize the multi-channel voltage pulses and timing marker generation. A high-frequency lock-in amplifier (Zurich Instruments, UHFLI) was used as a carrier generator and demodulator for homodyne detection. At room temperature, a carrier power of  $-40$  dBm was generated which was further attenuated by  $-50$  dB by the cryogenic attenuators and the directional coupler. The reflected signal is initially amplified by 50 dB with the cryogenic amplifier (Caltech Microwave Research Group, CITLF2 x2 in series), and then additionally amplified by 20 dB at room temperature using a custom-built RF amplifier. We used the QUA (Quantum Machines) language framework for scripting experimental sequences, performing single-shot readouts, and signal conditioning.

### Data availability

The data that support the findings of this study are available from the corresponding author upon request.

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### Author contributions

D.K. conceived and supervised the project. Y.S. and J.K. fabricated the device. Y.S., J.Y., and H.J. performed the measurements and analyzed the data with W.J. J.P., M.C., and H.S. built the experimental setup and configured the measurement software. S.M., N.U., and K.M.I. synthesized

and provided the  $^{28}\text{Si}/\text{SiGe}$  heterostructure. All the authors contributed to the preparation of the manuscript.

### Competing interests

The authors declare no competing interests.

### Additional information

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**Correspondence** and requests for materials should be addressed to Dohun Kim.

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